

Multi-Oriented Touching Text Character Segmentation in Graphical Documents using Dynamic Programming

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Abstract

The touching character segmentation problem becomes complex when touching strings are multi-oriented. Moreover in graphical documents sometimes characters in a single touching string have different orientations. Segmentation of such complex touching is more challenging. In this paper, we present a scheme towards the segmentation of English multi-oriented touching strings into individual characters. When two or more characters touch, they generate a big cavity region in the background portion. Based on the convex hull information, at first, we use this background information to find some initial points for segmentation of a touching string into possible primitives (a primitive consists of a single character or part of a character). Next, the primitives are merged to get optimum segmentation. A dynamic programming algorithm is applied for this purpose using the total likelihood of characters as the objective function. A SVM classifier is used to find the likelihood of a character. To consider multi-oriented touching strings the features used in the SVM are invariant to character orientation. Experiments were performed in different databases of real and synthetic touching characters and the results show that the method is efficient in segmenting touching characters of arbitrary orientations and sizes.

Keywords: Touching Character Segmentation, Multi-oriented Character Recognition, Dynamic Programming

1. Introduction

As electronic media becomes more and more accessible, the need for transferring offline documents to the electronic domain grows. Optical Character Recognition (*OCR*) works by scanning source documents and performing character analysis on the resulting images giving a transcription to ASCII text which can then be stored and manipulated electronically like any standard electronic document. As part of the OCR process, character segmentation techniques are applied to word images before individual characters images are recognized. The simplest way to perform character segmentation is to use the small space between characters as segmentation regions. This strategy fails when there are touching or broken characters, which often occur in degraded text images. Some examples of such documents are photocopies, faxes, historical documents, etc. and they are often degraded due to compression, bilevel conversion, aging or

14 poor typing [3, 28]. In these situations, two or more characters may be seg-
15 mented as one character component or one character may split into multiple
16 pieces. Due to degradation, adjacent characters in a word touch together and
17 they share common pixels in touching regions [27].

18 Besides the huge amount of documents having only horizontal direction text,
19 there are many graphical documents such as maps, engineering drawings, etc. or
20 artistic documents, where text lines appear frequently in different orientations
21 other than usual horizontal direction. The purpose of such orientation and
22 curvi-linearity is to catch people’s attention at some particular words/lines or to
23 annotate the location of graphical objects. Thus, a single document may contain
24 strings with different inter-character spacing in the strings due to the annotation,
25 style, etc. Also, the curvi-linear nature of the text makes the orientations of
26 characters in a string different. As a result, it is difficult to detect the skew of
27 such strings and hence character recognition of such documents is a complex
28 task.

29 Segmentation of touching components is one of the difficulties to get higher
30 recognition rates by OCR systems. The OCR systems available commercially
31 do not perform well when words are multi-oriented in fashion in a document.
32 When touching occurs in multi-oriented documents (e.g. artistic or graphical
33 documents), it is much more difficult to segment such multi-oriented touching
34 than touching segmentation of normal horizontal touching. Touching in curvi-
35 linear string leads to false character segmentation and hence wrong recognition
36 result occurs.

37 Text-lines could appear at different directions in the same document as illus-
38 trated in Fig.1. It can be seen from Fig.1(a), the word “PLANET” contains a
39 touching string “LANE” of four characters. In Fig.1(b), we show a map where
40 many characters in the word “Mayurakshi” are touching and they are oriented
41 in different directions, although they belong to a same word. Orientation of two
42 touching strings “ON” and “RE” of Fig.1(c) are perpendicular to each other.
43 In Fig.1(d), it may be noted that orientations of “es” and “no” in the word
44 “Cousesnon” are not the same and such strings create difficulty for segmenta-
45 tion.

46 1.1. Related Work

47 There are many published papers towards the recognition and segmentation
48 of the touching characters of horizontal direction [2, 15, 19, 30] and they are
49 briefly reviewed here.

50 Among the earlier pieces of work on touching character segmentation, one
51 class of approaches uses contour features of the connected components for seg-
52 mentation [7, 15, 29]. When analyzing the contour of a touching pattern, valley
53 and crest points are derived. Next, a cutting path is decided to segment the
54 touching pattern by joining valley and crest points. Kahan et al. [13] used pro-
55 jection profiles as the objective function for touching character segmentation.
56 They used the idea of joining adjacent characters that have minimum vertical
57 projection. The segmentation function is calculated from the ratio of the second
58 derivative of the projection-profile curve to its height. Later, Lu [18] introduced
59 a peak-to-valley function to improve the segmentation approach. Fujisawa et al.
60 [8] used profile features for touching numeral segmentation. Upper and lower
61 profiles of the connected component are computed and the distance between
62 upper and lower profiles are analyzed to detect the segmentation points.

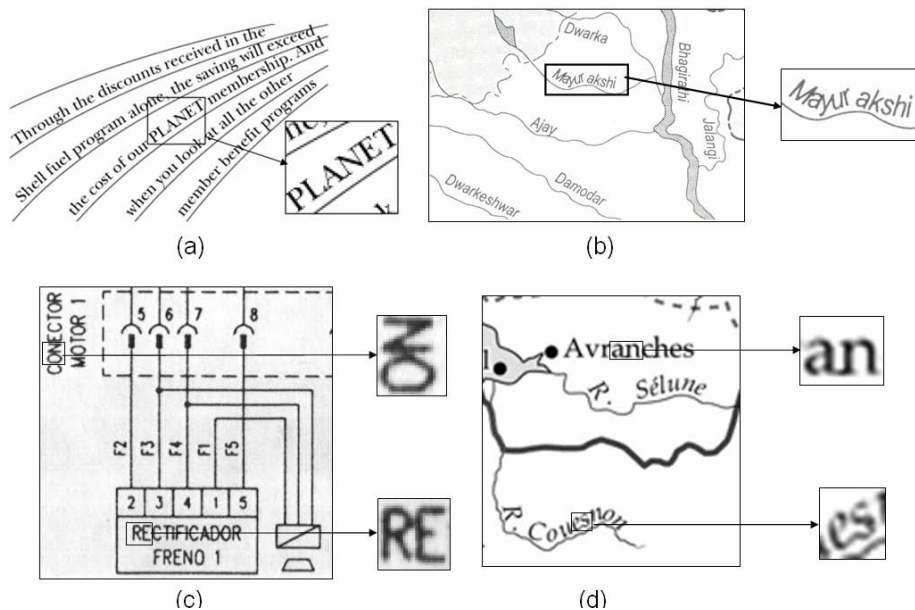


Figure 1: Example of documents showing multi-oriented touching characters in (a) an advertisement, (b) and (d) maps, and (c) electrical diagram.

63 Afterwards, Liang et al. [17] proposed discriminating functions for machine
 64 printed touching character segmentation. Pixel projection and profile projection
 65 techniques are employed as discrimination functions for solving heavily
 66 touching printed characters. Next, they applied forward segmentation along
 67 with a backward merge procedure based on the output of a character classifier.
 68 It works on the components generated by discriminating functions. Yu
 69 and Yan [32] presented a segmentation technique using structural features for
 70 single-touching hand-written numeral strings. At first, the touching region of
 71 the character components is determined based on its structural shape. Next,
 72 a candidate touching point is pre-selected using the geometrical information of
 73 special structural shapes. Finally, morphological analysis and partial recogni-
 74 tion results are used for the purpose of segmentation. Dimauro et al. [5] applied
 75 contour based features along with some descending algorithms for the touching
 76 character segmentation purpose.

77 Another class of approaches is based on thinning [3, 19]. In these approaches,
 78 thinning of foreground and/or background pixels of the connected pattern are
 79 processed. End and fork points obtained by thinning are used for cutting points
 80 extraction. These methods are time consuming and in addition they generate
 81 protrusions. These protrusions sometimes give wrong results because they bring
 82 some confusions among the actual fork and end points.

83 A water reservoir based technique [21] is employed to locate inter-character
 84 spaces in touching numeral strings. Water reservoir is a metaphor to illustrate
 85 the cavity region of a component. In this sense, if water is poured from a side
 86 of a component, the cavity regions of the background portion of the component
 87 where water will be stored are considered as reservoirs of the component. Based
 88 on the size of water reservoirs, the segmentation zones of the touching string

89 are selected. Next, segmentation is done using structural information of these
90 reservoirs.

91 Yong et al. [31] proposed an approach using supervised learning on the la-
92 beled examples and a Markov Random Field (MRF) approach has been applied
93 for this purpose. Further, a propagation minimization method is employed to
94 select the candidate patches based on the compatibility of the neighbor patches.
95 The output of the MRF after the iterative belief propagation forms a segmen-
96 tation probability map. Finally, the cut position is extracted from the map. An
97 accuracy rate of 94.8% is reported.

98 Methods based on combinations of features have also been used for touching
99 segmentation. Oliveira et al. [20] used contour, profile and skeleton features to
100 find a set of points for touching characters segmentation. First, local minima of
101 contours and profile features are defined as basic point (*BP*). Second, a point
102 with more than two pixels in its neighborhood is defined as an intersection
103 point (*IP*). Afterwards, an Euclidean distance scheme is applied to determine
104 proximity between *IP* and *BP* for segmentation.

105 The state-of-the-art approaches of touching character segmentation gener-
106 ally consider touching of characters in horizontal text strings. These methods
107 assume the characters of strings are aligned horizontally and thus segmen-
108 tation features are devised for such characters in horizontal strings. Also, the
109 features used in most of the approaches for text character recognition are gen-
110 erally not rotation invariant. The characters along a touching portion may be
111 in different orientations with respect to the baseline of the word. In graphical
112 documents when characters touch, it is difficult to know the angle of alignment
113 of characters in the touching regions. Moreover in Fig.1(b), we show examples
114 where the characters in a single touching have different orientations. As a result,
115 skew correction methods cannot make such touching horizontal and hence the
116 methods that take care of horizontal touching cannot be used. For segmen-
117 tation purpose, we need technique that can take care of size and rotation invariant
118 touching strings. Hence, we propose here a segmentation approach that can han-
119 dle touching strings in multiple orientations. Recently, we proposed a touching
120 character segmentation approach in ICDAR-2009 [25] and the present work is
121 its extended version. This paper elaborates the different steps of character seg-
122 mentation method. Also, extensive experiments including comparative study
123 are included in this version to prove the efficiency of this method.

124 1.2. Outline of the Proposed Approach

125 As mentioned earlier, many techniques are available for segmentation of
126 horizontal touching characters but to the best of our knowledge there is no
127 work towards multi-oriented touching character segmentation except our work.
128 In this present paper, we propose an approach for multi-oriented n-character
129 touching string segmentation scheme. The block-diagram of our approach is
130 shown in Fig.2. The different steps used in this system are discussed as follows.

131 *Recognition process:* An important step in our system is the recognition
132 of the isolated character. As we consider multi-oriented graphical document,
133 features used in our system must be rotation invariant. Circular and convex
134 hull ring based zoning approach has been used along with angular information
135 of the contour pixels of the character to make the feature rotation invariant.
136 A SVM classifier is used to find the likelihood of a character. The C1 and C2
137 modules of Fig.2 discuss about recognition.

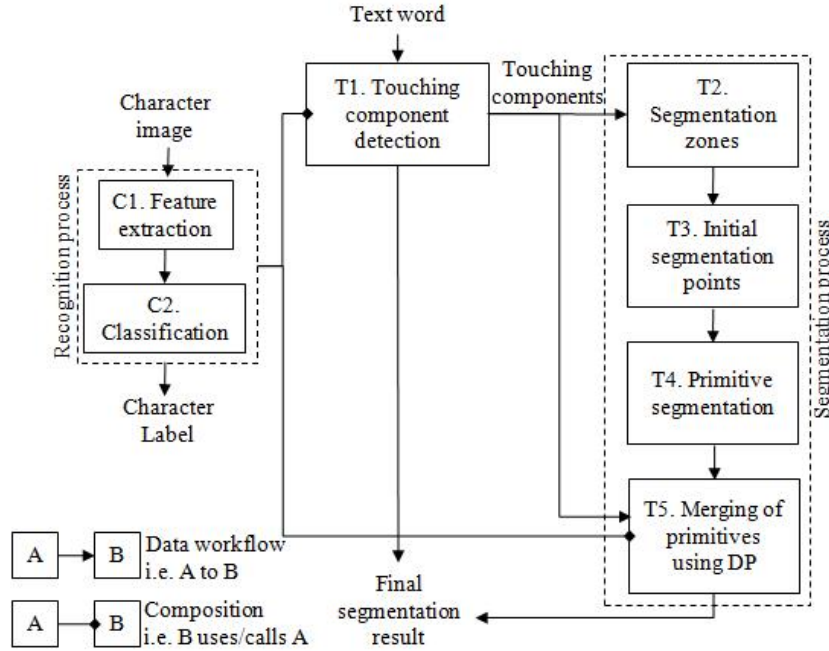


Figure 2: Block diagram of the proposed approach for touching character segmentation.

138 *Touching component detection:* There may exist touching or non-touching
 139 characters in a word. Before passing a component into our segmentation process
 140 (steps T2-T5 of Fig.2), we detect if the component is touching or isolated. We
 141 apply a Connected Component (CC) labeling to the word image and extract
 142 individual components. For each component, we compute the recognition confi-
 143 dence for all character class models using our recognition process (steps C1-C2).
 144 Based on this recognition score, the components are separated into touching and
 145 non-touching components. The touching components are processed next for seg-
 146 mentation. This module is noted by T1 in Fig.2 and discussed later.

147 *Segmentation zones:* When two or more characters touch, they generate a
 148 big cavity region at the background portion. This background portion is used
 149 to detect the segmentation zones. To handle the background information of a
 150 multi-oriented string, properties of the convex hull of the touching string have
 151 been used. This process is marked by T2 in Fig.2.

152 *Initial segmentation points:* The segmentation zones are used to find the
 153 segmentation points. A set of initial segmentation points are calculated in the
 154 contours of convex hull residua using the Douglas Peucker polyline approxima-
 155 tion. This is denoted by T3 in Fig.2.

156 *Primitive Segmentation:* Next, segmentation lines are calculated from the
 157 initial segmentation points of the touching character. Based on these segmenta-
 158 tion lines, the touching string is segmented into primitives. A primitive consists
 159 of a single character or a part of a single character. This step is mentioned by
 160 T4 in Fig.2.

161 *Merging of primitive segments using dynamic programming:* Some of the
 162 primitives obtained before are merged to get optimum segmentation. To do this,

163 dynamic programming algorithm is applied using total likelihood of characters
164 as the objective function. Based on the recognition rates of primitive segments,
165 multiple hypothesis of segmentation are generated. A dynamic programming
166 (DP) algorithm is applied to get the optimal solution for the touching character
167 segmentation. This step is marked by T5 in Fig.2.

168 As discussed earlier, the main contribution of this paper is the multi-oriented
169 n-character string segmentation for its recognition (i.e. steps T2-T5 in Fig.2).
170 However, it is difficult to dissociate this part from the recognition process. So,
171 we will present recognition procedure briefly before detail discussion of touching
172 character segmentation.

173 The rest of the paper is organized as follows. In Section 2, we explain
174 the feature extraction procedure as well as recognition for handling characters
175 in multi-scale and multi-oriented environments (steps C1 and C2 of Fig.2). In
176 Section 3, we present the proposed segmentation approach for n-touching strings
177 (steps T1-T5 of Fig.2). Next, data details and the different experimental results
178 are discussed in Section 4. Finally, the paper is concluded in Section 5.

179 2. Feature Description and Recognition of Text Character

180 Recognition of text characters in multi-rotation and multi-scale environment
181 is a challenging task. Recognition of individual characters in multi-oriented
182 and multi-sized environment drives the segmentation hypothesis of n-touching
183 characters in our system. In the literature different shape descriptors like An-
184 gular Radial Transform (ART) [23], Hu’s moments [12], Zernike moments [14],
185 Fourier-Mellin [1], Angle based features [22] etc. are proposed for recognition
186 and they are invariant to rotation, translation and scale. We noted that an an-
187 gles based feature provides best performance among different rotation invariant
188 shape descriptors. Because of the highest performance we have used an angle
189 based feature for our work. The computation of such feature is briefly described
190 in the following subsections.

191 2.1. Feature Descriptor

192 Our *Angle based feature* descriptor is a zone-wise feature descriptor to de-
193 scribe symbol/text characters. It is based on the histogram of angular informa-
194 tion of the external and internal contour pixels of the characters. The relative
195 angles obtained from all the contour pixels of a character are grouped into bins.
196 Here, we consider 8 bins ($360^\circ/45^\circ$) of angular information.

197 To obtain local relative angle information, circular ring and convex hull
198 rings are constructed. A set of circular rings is defined as the concentric circles
199 considering their center as the center of Minimum Enclosing Circle (MEC) of
200 the character and the minimum enclosing circle is the outer ring of the set.
201 Similarly, convex hull rings are also constructed from the convex hull shape of
202 the character. Angular slope of the contour pixels with respect to the center of
203 the MEC is also included as rotation invariant features. The slope of contour
204 pixels for each bin is computed and grouped into different sets. Details of feature
205 explanation can be found in [22], so we are elaborating it here.

206 Considering 7 circular rings and 7 convex hull rings, we have 56 (8 relative
207 angular bins \times 7 convex hull rings) features from the convex hull ring, 56 (8
208 relative angular bins \times 7 circular rings) features from the circular ring and 64

209 (8 relative angular bins \times 8 sets of angular slopes) features from angular slope
210 with respect to the center of MEC. As a result, we have a 176 (56+56+64)
211 dimensional feature vector for the classification. The numbers of bins, rings and
212 sets have been selected based on the experiment. To obtain scale invariance,
213 the feature vector is normalized. The feature vector is divided by the total
214 number of contour pixels for this purpose. We have shown the plot of 176
215 dimensional features of characters between intra-class and inter-class characters
216 in Fig.3. From the figure it can be seen that the corresponding features of same
217 character classes are similar although the characters are multi-oriented.

218 2.2. Character Recognition

219 A Support Vector Machine (SVM) has been used to build the isolated character
220 models. We employed the SVM software package *libSVM*¹ for this purpose.
221 A Gaussian kernel with Radial Basis Function (*RBF*) has been chosen in our
222 system to recognize multi-oriented text characters. Feature learning is done with
223 datasets of multi-oriented characters to generate the text character models.

224 During the training process, the SVM generates character models according
225 to pre-segmented text characters. After training, when an unknown character
226 or a primitive segment is fed to this SVM classifier, the SVM provides its class
227 label along with its weight. The value of the weight lies between 0 to 1. We
228 consider this weight as recognition confidence and this value is used as the cost
229 function in our dynamic programming approach for correct segmentation of
230 multi-oriented touching characters.

231 3. Touching Character Segmentation

232 A touching component segmentation approach for two touching characters
233 in a multi-oriented environment was presented in [24]. This segmentation was
234 performed with the knowledge of the number of total characters in the touching
235 component. To do this, touching components of only 2 characters were collected
236 and the method was based on cavity regions of the background portion. The
237 convex hull was used to find the cavity regions. Next, several hypothesis of
238 segmentation lines were computed from these cavity regions. Each of these
239 segmentation lines divided the touching component into 2 parts. Finally, all
240 pair-wise segmented parts were fed to the SVM classifier to find the correct
241 segmentation. The best segmentation line was selected based on the highest
242 accumulated recognition confidence of the two parts of the touching component.

243 Continuing with this idea, a touching component of n-characters could be
244 segmented if the number of character in the touching component were known
245 before. This concept is restricted because we have to know the number of
246 characters in the touching component a priori. It is a hard constraint, since
247 it is not always possible to know the number of characters in a real touching
248 component in a multi-scale and multi-rotation environment. Because of this,
249 here in this paper, we propose an optimization algorithm to segment n-character
250 touching components.

251 If a n-character string or word is rotated to a certain angle, we estimate
252 a rough angle from the minimum rectangular bounding box of the string. We

¹<http://www.csie.ntu.edu.tw/~cjlin/libsvm/>

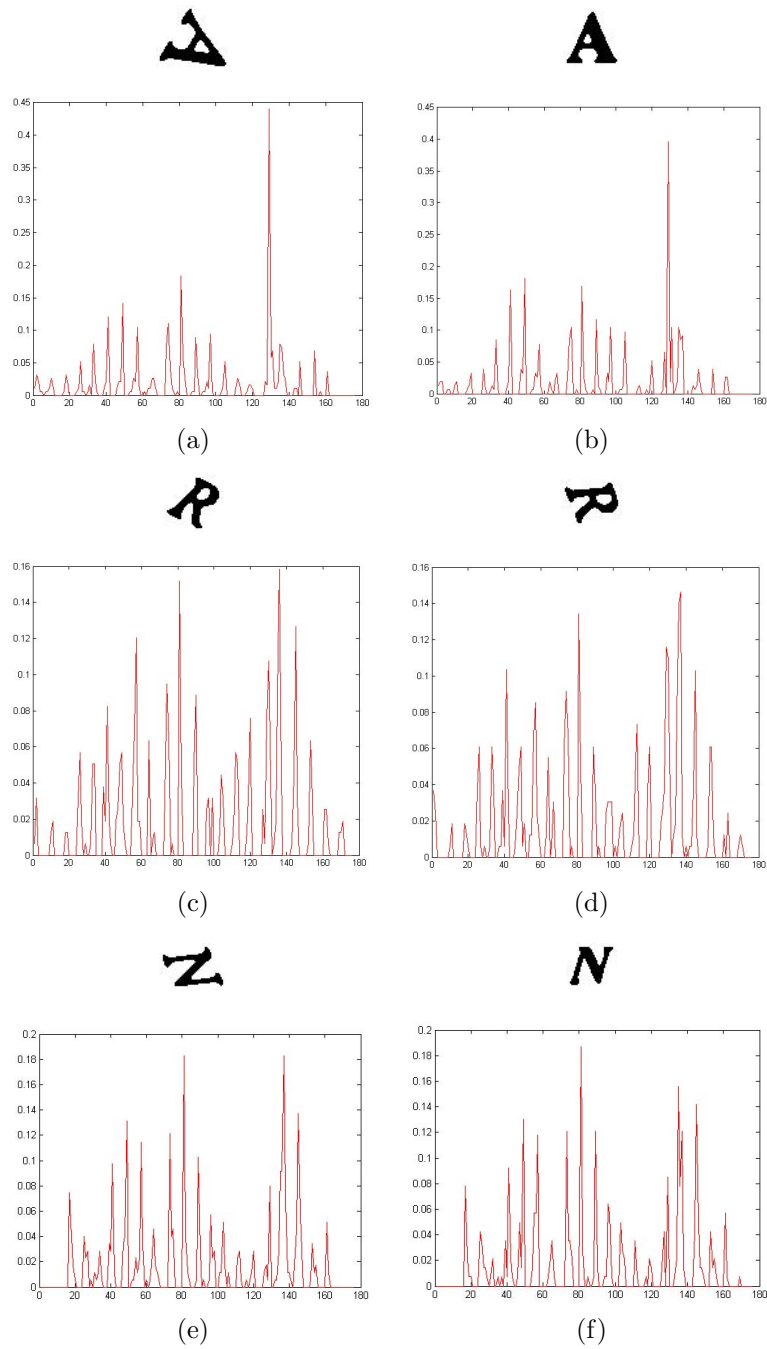


Figure 3: Feature vectors are plotted for different orientations of characters 'A', 'R' and 'N'. (Here, X axis (horizontal) denotes the feature vector and Y axis (vertical) denotes their values.)

253 compute the bounding box of the word and find the angle (α) of the major
 254 axis. Better approximation of the angle can be obtained if a word contain more

255 number of characters. An approximate height of the word (H_w) is found from its
 256 bounding box (See Fig.4). It is to be noted that, when there are few characters in
 257 the word and it includes characters having ascenders and descenders, α indicates
 258 an approximated angle of the inclination of the word. In Fig.4, we show a multi-
 259 oriented word along with its bounding box and α and H_w are marked in this
 260 figure. It can be noted that if this word is rotated by α then all the components
 261 of the word will not be in horizontal mode. Hence, existing approaches of
 262 horizontal touching character segmentation can not be applied in such string
 263 after rotating it by α . Given a touching string of unknown orientation, our rough
 264 inclination angle α is used to arrange the primitive segments of the touching
 265 component in a sequential order, such that a dynamic programming algorithm
 266 can be applied to merge some of the primitive segments for proper segmentation.

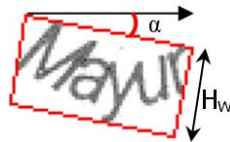


Figure 4: A multi-oriented word and its bounding box are shown. Here, α indicates the rough angle of inclination and H_w is the height of the bounding box.

267 Our proposed segmentation method is divided into five main steps (See
 268 Fig.2): touching component detection (T1), segmentation zones (T2), initial
 269 segmentation points (T3), primitive segmentation (T4) and merging of primi-
 270 tive segments using DP (T5). Details of the segmentation method are discussed
 271 in the following subsections.

272 3.1. Touching Component Detection

273 There may exist touching or non-touching characters in a word. A compo-
 274 nent is detected as touching or isolated before applying the segmentation
 275 approach on the touching string. For this purpose, at first, a Connected Com-
 276 ponent (CC) labeling is applied to extract individual components of the word.
 277 For each component, we compute the recognition confidence for all character
 278 class models using SVM and rank their confidence scores in descending order.
 279 If a component is recognized by the SVM with a high accuracy (more than 0.4),
 280 we assign it as a non-touching or isolated character. If the difference between
 281 the top two recognition scores of a component is high, it is also considered as
 282 an isolated character. The rest of the components are considered as touching.
 283 These touching components are processed for segmentation using our approach.
 284 We may get some false positive labelling due to such separation based on confi-
 285 dence score. For example, the difference between the top two recognition scores
 286 may be less for characters like ‘D’ and ‘O’. Such mislabelled components do not
 287 affect the final segmentation result because the proposed dynamic programming
 288 approach takes care of such errors with the final optimal score.

289 3.2. Segmentation Zones

290 When two or more characters touch, generally they generate big cavity re-
 291 gions at the background portion between touching components. When compo-
 292 nents in a string are in the horizontal direction, the water reservoir concept can

293 be used to find these cavity regions [21]. Water reservoir based algorithms may
 294 not be applied in the strings of multi-oriented nature. We have considered some
 295 properties of the convex hull to take care of this problem.

296 The Convex Hull [10] or convex envelope for a set of points X in a real vector
 297 space V is the minimal convex set containing X . In another way, a convex hull
 298 is a minimal convex shape entirely bounding an object. Some of the properties
 299 of convex hull residuum are described as follows.

- 300 1. Residuum area (R_A): The area of a residuum is defined by the number of
 301 pixels inside the residuum.
- 302 2. Residuum surface level (R_{SL}): The R_{SL} of a residuum is the line obtained
 303 by joining two endpoints of the open face of the residuum.
- 304 3. Residuum border pixels (R_{BP}): The border pixels of each residuum are
 305 defined as the contour pixels of the residuum excluding the R_{SL} pixels.
- 306 4. Residuum height (R_H): It is the depth of the farthest residuum border
 307 pixel from R_{SL} .

308 In Fig.5, convex hull residua and their different parameters for a text character
 309 ‘S’ are shown.

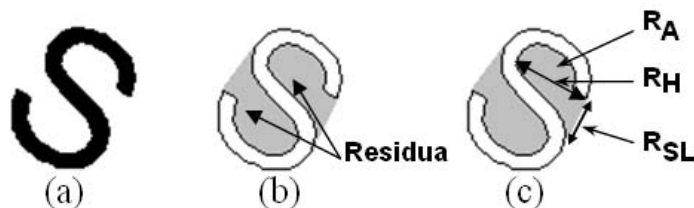


Figure 5: (a) Image of the character ‘S’. (b) Two residua from the convex hull of ‘S’. (c) Different parameters of convex hull are shown in a residuum.

310 Similarly, the cavity regions of the touching component are determined by
 311 finding residua of that component through convex hulls. These residua cover
 312 the cavity regions of the touching component and thus, they are used to de-
 313 termine the segmentation zone of touching characters. The residua found from
 314 the convex hull of a touching character are shown in Fig.6. For this touching
 315 component (“72”), we find a total of four cavity regions.

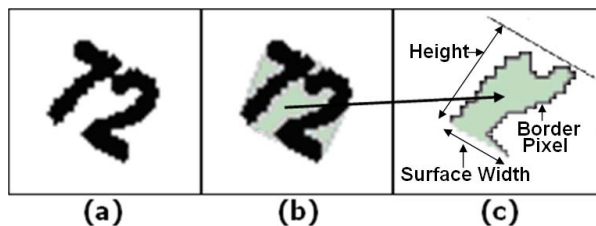


Figure 6: (a) Touching character. (b) The residua of the convex hull are shown and marked by grey shade. (c) Different parameters of the residuum.

316 Given a touching component, we may find many small cavity regions along
 317 with the segmentation zones due to the degradation of contour of the characters.
 318 Even, the presence of “Serif” in some fonts of text characters (e.g. Times New

319 Roman) also produces small cavity regions. These small cavity regions are
 320 considered as noise and thus, these are not considered for segmentation in this
 321 approach. To do that, the residua having height more than stroke-width are
 322 considered for segmentation purpose. The stroke-width (St_w) of the word is
 323 the statistical mode of object pixels' run lengths [2]. For a component, St_w
 324 is calculated as follows. The component is scanned row-wise (horizontally),
 325 column-wise (vertically) and then in two diagonal directions (45° and 135°). If
 326 rl different runs of lengths $r_1, r_2 \dots r_{rl}$ with frequencies $f_1, f_2 \dots f_{rl}$, respectively
 327 are obtained by the scanning the component, then value of St_w will be r_i if f_i
 328 $= \max(f_j), j = 1, 2 \dots rl$.

329 3.3. Initial Segmentation Points

330 To segment a touching string into possible primitive segments, segmentation
 331 points are next computed from the segmentation zones extracted previously. To
 332 do it, we employ a polygonal approximation method to the contour pixels of
 333 residuum borders. Polygonisation provides key-points which are at the corner
 334 of edges in the corresponding segmentation zones. Among existing algorithms
 335 of the literature [16], we have selected the Douglas and Peucker [6] polygonal
 336 approximation algorithm. A short presentation of this algorithm is given in
 337 Appendix A. This algorithm is well adapted to localize hard curvature points
 338 along a border.

339 The two end points of the residuum surface level (R_{SL}) of each selected
 340 residua are regarded as the initial rough estimate of the polyline. Using this
 341 initial guess, the other vertices are approximated using a tolerance threshold
 342 ϵ . The value of this tolerance threshold is selected with stroke width (St_w)
 343 precision. After approximation, the list of vertices are treated as key-points. The
 344 advantage of using polygonal approximation is that it provides the key-points
 345 which are at the corner of the edges in the corresponding segmentation zones.
 346 These key points are necessary for touching character segmentation because,
 347 usually when the characters touch, they form a corner at the touching region.

348 We have noted that some of the key-points might appear very near to R_{SL}
 349 due to the appearance of hard curvature or degradation in the contours of these
 350 zones. These key-points do not provide the segmentation lines and thus are
 351 selected for removal. We remove such key-points based on the corresponding
 352 residuum height (R_H). The key-points which are having height more than
 353 $(0.5 \times R_H)$ from the corresponding R_{SL} are kept for the initial segmen-
 354 tation points. Remaining key-points are considered as the initial segmentation
 355 points. In Fig.8(b), we have shown the initial segmentation points for the image
 356 Fig.8(a). Similarly, these initial segmentation points are shown for a touching
 357 component of fonts having serifs in Fig.7.



Figure 7: A touching component of characters "UT" is shown with its initial segmentation points. These initial segmentation points are marked in dark gray (red in pdf).

358 *3.4. Primitive Segmentation*

359 Once we get initial segmentation points, for each initial segmentation point
 360 (S_i) we find another point (S_j) through which the touching component can be
 361 cut into 2 parts. Computation of S_j is done as follows. We know the angle of
 362 the direction of the R_{SL} with the horizontal axis. For each initial segmentation
 363 point, we find a segmentation line passing through this point and perpendicular
 364 to the respective R_{SL} . This line segments a touching component at the point
 365 S_i . The perpendicular line to the R_{SL} generally gives us a clue to the direction
 366 of the segmentation line. We draw a line from the point S_i in the opposite
 367 side of R_{SL} and perpendicular to the R_{SL} until it passes through the object
 368 pixels. Let, the last object pixel on this line be S_c . The line from S_i to S_c
 369 may be considered as a segmentation line. This segmentation line may not
 370 give the best segmentation always and hence to get better segmentation the
 371 point S_c is tuned to be a better segmentation point. This tuning is done by
 372 considering some neighbor contour points of the point S_c . To get neighboring
 373 pixels, the contour is traced upto a length of stroke-width (S_w) clockwise and
 374 anti-clockwise starting from S_c . These traced pixels are neighbor pixels. The
 375 neighbor pixel having the minimum distance from S_i is chosen as S_j . The line
 376 obtained by joining S_j and S_i is the segmentation line and the distance between
 377 S_j and S_i is called the length of segmetnation line. We explain the segmentation
 378 line computation process in Algorithm 1.

Algorithm 1 Segmentation Lines of Touching Component

Require: Touching component (C_T)

Ensure: A set of segmentation lines from C_T

 Compute convex hull of C_T and find the residua.

 //create a list (L_S) of segmentation lines

$L_S \leftarrow \emptyset$

for all residua R_k of C_T **do**

 Generate the initial segmentation points using polyline approx. in the
 contour of R_k

for all initial segmentation points S_i **do**

 Compute segmentation line (L_{ik}) at S_i perpendicular to R_{SL} of R_k and
 tune L_{ik}

$L_S \leftarrow L_S \cup L_{ik}$

end for

end for

379 It may happen that the touching portion of the components creates segmen-
 380 tation zones in both sides (top and bottom) of the characters. Such touching
 381 creates multiple hypotheses of segmentation points in both sides. These points
 382 generate segmentation lines for the components. As a result, some of the seg-
 383 mentation hypotheses may lie very close to other. To reduce the choices of
 384 hypotheses we remove some of the lines which are very closed. If the distance
 385 between two segmentation lines is less than S_t_w , the segmentation line with
 386 bigger length is not considered for segmentation. Moreover, if the length of a
 387 segmentation line is greater than $0.75 \times H_w$, that segmentation line is also not
 388 considered. This value is determined from the experimental result.

389 For each initial segmentation point we get the corresponding segmentation
 390 line. If we have n segmentation lines, the image is segmented into $(n + 1)$

391 sub-images. The (candidate) segmentation lines of Fig.8(a) have been shown
 392 in Fig.8(c). Note that, there were 7 initial segmentation points (See Fig.8(b))
 393 and we have got 5 segmentation lines (these 5 segmentation lines are shown in
 394 Fig.8(c)). These segmentation lines split the touching component into primitive
 395 segments. In Fig.8(c) there are 6 primitive segments. These primitive segments
 396 are arranged in a sequence following the direction of angle α . Now, we will merge
 397 some primitive segments for correct segmentation. A dynamic programming
 398 technique is used for the purpose.

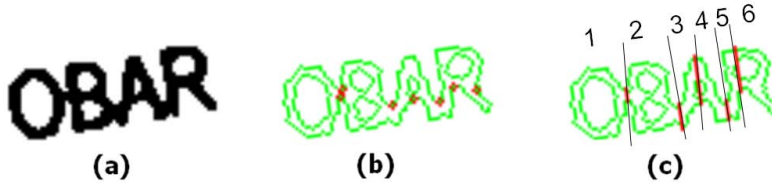


Figure 8: (a) A touching string of four characters. (b) Initial segmentation points found from concave residua. (c) Candidate segmentation lines and primitive segments obtained from selected segmentation points.

399 3.5. Merging of Primitive Segments using Dynamic Programming

400 The key idea behind dynamic programming (DP) is quite simple and the
 401 core of a DP algorithm [9] is the module that takes a set of symbols (list of
 402 primitive segments in our case) and a set of labels (possible characters) and
 403 returns the optimum assignment of labels to symbols assuming that an optimum
 404 assignment is the sum of the sub-assignments (sub-problems). DP is a very
 405 powerful algorithmic paradigm in which a problem is solved by identifying a
 406 collection of sub-problems and tackling them one by one, smallest first, using
 407 the answers to small problems to help figure out larger ones, until the whole lot of
 408 them is solved. The DP seeks to solve each sub-problem only once, thus reducing
 409 the number of computations. Given a touching image, the primitive segments
 410 are merged so that the average character likelihood is maximized using DP and
 411 in our case, the likelihood of each character is calculated using a recognition
 412 accuracy obtained by the SVM. Generally the order of time complexity of DP is
 413 $O(N \times M \times M)$, where N is the length of the touching string and M is maximum
 414 number of primitive segments for a character. From, our experiment we noted
 415 that a single character can take at most four primitive segments and hence, M
 416 reduces to four in our case.

417 To apply the DP algorithm, the primitive segments are arranged from left
 418 to right following the direction of α . Let S_1, S_2, \dots, S_n be a list of n primitives. In
 419 Fig.8(c) the six primitive segments ($n = 6$) are indexed according to their sorting
 420 order. We use two tables to store the character likelihood of primitive segments
 421 after merging (see Fig.9). In the Score Table ST , we enter the classification
 422 score $\{c_{uv}\}$ and in the Label Table LT , we enter the character classification
 423 label $\{l_{uv}\}$ where $1 \leq u \leq v \leq n$. The classification scores and classification
 424 labels are defined as follows:

$$c_{uv} = \bigcup_{i=u}^v S_i \quad , \text{ score from ST}$$

425

$$l_{uv} = \bigcup_{i=u}^v S_i \quad , \text{ label from LT}$$

426 In these tables, the cells correspond to the recognition result of a cumulative
 427 grouping of primitive segments. The possible merging result of the primitive seg-
 428 ments of Fig.8(c) are shown in Fig.9(a) and Fig.9(b). For example, in Fig.9(b),
 429 the cell l_{35} represents the character likelihood of merging the primitive segments
 430 S_3, S_4 and S_5 . The label obtained by our SVM is ‘ m ’. In table ST, the cell c_{35}
 431 indicates the corresponding classification score (0.183) to obtain the label ‘ m ’.
 432 If the classification score of merged segments is very low (a threshold value of
 433 0.1 is decided empirically), we do not consider it. Cumulation of primitive seg-
 434 ments is continued until the width of the resultant image is less than $1.2 \times H_w$.
 435 This value is chosen based on the size of the Latin alphabet. Also, characters
 436 like ‘M’ can be segmented into multiple hypothesis of ‘1’. So, if we find two or
 437 more consecutive character shapes of ‘1’, ‘t’, etc., we check the hypothesis of
 438 the combination of these shapes and based on the recognition confidence, the
 439 character is selected.

		v (merged primitives) →					
		S1	S2	S3	S4	S5	S6
u (starting primitive) ↓	S1	0.969					
	S2		0.856	0.705			
	S3			0.566	0.380	0.183	
	S4				0.266	0.645	0.245
	S5					0.158	0.839
	S6						0.103

(a)

		v (merged primitives) →					
		S1	S2	S3	S4	S5	S6
u (starting primitive) ↓	S1	O					
	S2		B	a			
	S3			t	A	m	
	S4				t	n	m
	S5					l	R
	S6						2

(b)

Figure 9: (a) Score Table ST and (b) Label Table LT of character string “OBAR”.

440 Next, we check the total likelihood of the character groups. The group hav-
 441 ing the maximum likelihood is chosen and the corresponding merged primitives
 442 are their segmentation result. In Fig.8(c), the first segment corresponds to the
 443 letter ‘O’, the second segment corresponds to the letter ‘B’, the third and the
 444 fourth segments correspond to the letter ‘A’ and the fifth and sixth segments
 445 correspond to the letter ‘R’. The assignment of primitive segments for the char-
 446 acters $O B A R$ is also represented by:

$$447 \quad i \rightarrow 1 \ 2 \ 3 \ 4 \quad \text{and} \quad j(i) \rightarrow 1 \ 2 \ 4 \ 6$$

448 where i denotes the letter number, $j(i)$ denotes the number of the last primitive
 449 corresponding to the i -th letter. Note that the number of the first primitive
 450 segment corresponding to the i -th letter is $j(i-1) + 1$. Given $j(i)$, ($i = 1 \dots n$),
 451 the total likelihood of characters is represented by

$$L = \sum_{i=1}^n l(i, j(i-1) + 1, j(i)) \quad (1)$$

452 where $l(i, j(i-1) + 1, j(i))$ is the likelihood for the i -th letter. The optimal
 453 assignment (the optimal segmentation) that maximizes the total likelihood is
 454 found in terms of dynamic programming as follows. The optimal assignment
 455 $j(n)^*$ for the n -th letter is the one such that

$$L_{j(n)}^* = L(n, j(n)^*) = \text{Max} L(n, j(n)) \quad (2)$$

456 where $L(k, j(k))$ is the maximum likelihood of partial solutions given $j(k)$ for
 457 the k -th letter. This is defined and calculated recursively by

$$\begin{aligned} 458 \quad L(k, j(k)) &= \text{Max}_{j(1), j(2) \dots j(k-1)} \sum_{i=1}^k l(i, j(i-1)+1, j(i)) \\ &= \text{Max}_{j(k-1)} [l(k, j(k-1) + 1, j(k)) + L(k-1, j(k-1))] \end{aligned} \quad (3)$$

$$459 \quad \text{and} \quad L(0, j(0)) = 0 \quad \text{for} \quad j(0) = 1, 2, \dots, m \quad (4)$$

460 Starting from (4), all $L(k, j(k))$'s are calculated for $k = 1, 2, \dots, n$ using (3) to
 461 find $j(n)^*$ using (2). The rest of $j(k)^*$'s ($k = n-1, n-2, \dots, 1$) are found by back
 462 tracking a pointer array representing the optimal $j(k-1)^*$'s which maximizes
 463 $L(k, j(k))$ in (3).

464 Given a segment group, the feature vector is calculated for a character class.
 465 Based on the character likelihood, the total likelihood of a word is found in
 466 terms of the dynamic programming technique discussed above. In Fig.10 we
 467 have shown the final segmentation result of the touching characters of Fig.8(a).



Figure 10: Final segmentation lines are drawn on the touching string shown in Fig.8(a) after applying our proposed approach.

468

469 4. Data Collection and Experimental Results

470 In this section we detail the performance of the proposed approach. First we
 471 describe the dataset generation and then we show experimental results of our
 472 touching character segmentation approach.

473 4.1. Dataset Generation

474 To the best of our knowledge, there exists no standard database to evaluate
475 character segmentation methods in a multi-oriented and multi-size context. For
476 our experiments, we have constituted our own database using real as well as syn-
477 thetic data. Synthetic data is available online¹ for the use of other researchers.

478 The real data is collected from maps, newspapers and magazines. We have
479 considered 10 different real geographical maps for evaluation of OCR in graphi-
480 cal documents. The average size of these map images are 1200×1200 . There
481 are approximately 35-40 words in each document. Documents are digitized in
482 grey tone at 300 dpi and we have used a histogram based global binarization
483 algorithm for their two tone conversion. A text separation method [26] has
484 been used to extract characters from documents, and the groundtruth has been
485 generated manually.

486 Synthetic data is generated from Arial and Times New Roman fonts. Some
487 of them are shown in Fig.12(a) and (b). These datasets have been produced
488 using the system described in [4]. The data are produced at first in vector
489 graphics form with the corresponding ground-truth. Next, vector graphics data
490 are rasterized to obtain the test images. The touching strings are composed
491 of single-word images with different scales, orientations and fonts, with cor-
492 responding groundtruth at the character level. The words are selected from a
493 dictionary (of 52 country names), with random scaling and rotation parameters.
494 The average number of characters in the word is 7-8. In each word, this data
495 generation method looks for the pairs of successive characters, and makes them
496 connected according to a boolean value. The overlapping between characters is
497 controlled using a Gaussian function.

498 In our experiment on touching character segmentation, we tested our scheme
499 on 450 words (200 real and 250 synthetic). The synthetic data contains touching
500 as well as non-touching characters. There were 880 touching components in
501 these 450 words. Also we noted that 2050 characters touched in these 880
502 touching strings. The touching strings are of different sizes and orientations.
503 Some of the data are up side down to check the rotation invariance nature of
504 our method.

505 4.2. Isolated Character Recognition using Different Shape Descriptors

506 Isolated text recognition in a multi-scale and multi-oriented environment
507 drives the solution towards the touching character segmentation problem. Text
508 character recognition is a challenging task in such an environment. To over-
509 come such problems, multi-scale and multi-rotation shape features are used as
510 discussed in Section 2. A SVM classifier with *RBF* function is employed for
511 isolated text character recognition.

512 In our experiment both English uppercase and lowercase alpha-numeric char-
513 acters are considered, so we should have 62 classes (26 for uppercase, 26 for
514 lowercase and 10 for digits). But because of shape similarity due to orientation
515 some of the characters like ‘d’ and ‘p’; ‘b’ and ‘q’; etc. are grouped together.
516 Hence, in our approach we considered 40 classes of character shapes. Different
517 fonts of characters including Times New Roman and Arial have been used for
518 the experiment.

¹<http://mathieu.delalandre.free.fr/projects/sesyd/charseg.html>

519 A comparison is done with other rotation invariant feature descriptors used
520 in the literature, namely: ART, HU, Zernike moments and Fourier Mellin. We
521 considered three different sets of data consisting of multi-oriented and multi-
522 scale text characters to perform this character recognition evaluation. One of
523 the datasets is from graphical documents and its size is 8250. The groundtruth
524 of this dataset has been generated manually for the performance evaluation. The
525 other two datasets are synthetic data, constructed from Arial and Times New
526 Roman fonts characters. The size of both of these datasets is 1850. The feature
527 vectors obtained from different descriptors are passed to a SVM classifier to get
528 the recognition accuracy. The classification is done with 5-fold cross-validation.
529 Comparative results of different descriptors are shown in Fig.11. It is noted
530 that angle based features (HU moments) perform the best (worst) among these
531 descriptors to classify text characters.

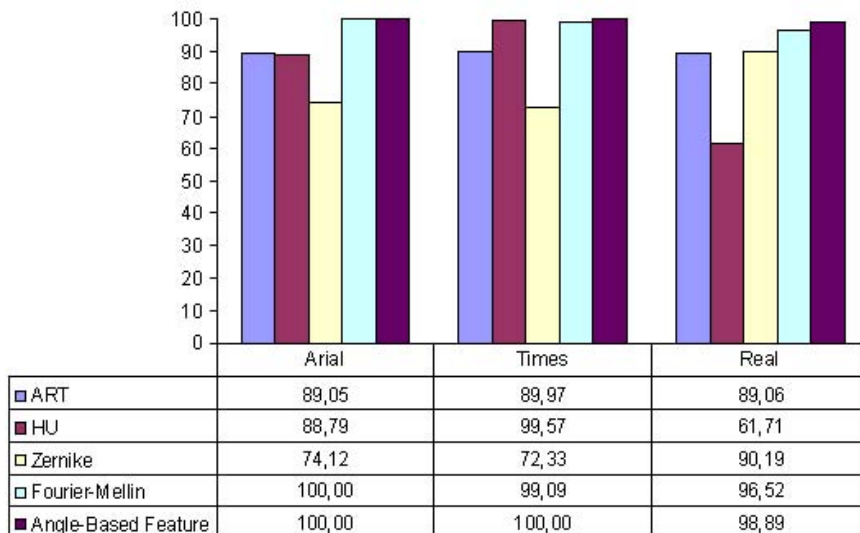


Figure 11: Text character recognition accuracy with different shape feature descriptors like ART, HU, Zernike, Fourier Mellin and Angle based feature.

532 4.3. Performance Evaluation of n -Touching Characters

533 In our experiment, here at first, we have provided some qualitative results
534 to show how segmentation is done with our approach. Next, we evaluate the
535 performance of our method in the datasets discussed in Section 4.1. To get
536 an idea about the segmentation results, we have shown some touching images
537 with their segmentation results in Fig.12. In Fig.12(c), some of the words are
538 touching in a curvilinear fashion. Our method also segmented them correctly.

539 We compared the touching character segmentation results using 2 different
540 multi-oriented text descriptors namely: angle based features and Fourier-Mellin
541 moments. The Fourier-Mellin moment shape descriptor has been chosen due to
542 its good performance in recognizing isolated multi-oriented characters [1]. We
543 obtained 91.36% and 88.38% segmentation accuracy in overall experiment using
544 angle based features and Fourier-Mellin, respectively. In Table 1, we provide



(a)



(b)



(c)

Figure 12: Some segmentation results of different datasets when angle based features are applied : (a) Arial font (b) Times New Roman font (c) Real data.

545 the accuracy of touching character segmentation based on the number of char-
 546 acters present in a touching component. We noted that, our system provides
 547 better results on 2-character touching strings than 3 or more character touching
 548 strings. Fig.13 provides the comparative results of different datasets using these
 549 two different features. It can be noted that angle based features provides better
 550 segmentation results than that of Fourier Mellin in all these datasets.

551

552 **Error Analysis:** Fig.14 shows some wrong segmentation of touching char-
 553 acters from our method. It is noted that most of the segmentation errors are

554 due to following. (a) When a touching string can be segmented in more than
555 two ways to get the valid segmented characters. For example, in Fig.14(a) the
556 touching string was formed from the characters ‘r’ and ‘m’. But this touching
557 string can be visualized as ‘r-r-n’ also, and our system segmented this string into
558 ‘r’, ‘r’ and ‘n’ instead of ‘r’ and ‘m’ which we consider as erroneous. (b) The
559 character shapes like ‘h’ (Fig.14(b)) may be split in two parts and our system
560 segments this character into ‘t’, ‘l’. We also considered it as wrong segmentation.
561 (c) Since our method is based on convex hulls, when touching is made in two or
562 more positions, we may not find any segmentation point in the touching cavity
563 region. Hence we get erroneous results.

Table 1: Segmentation results on touching string of different length.

No. of characters in a touching string	Total number of touching strings	Segmentation Accuracy	
		Angle-based	Fourier-Mellin
2	635	92.60%	91.18%
3	206	89.97%	86.25%
≥ 4	38	86.18%	73.68%
Total	879	91.36%	88.38%

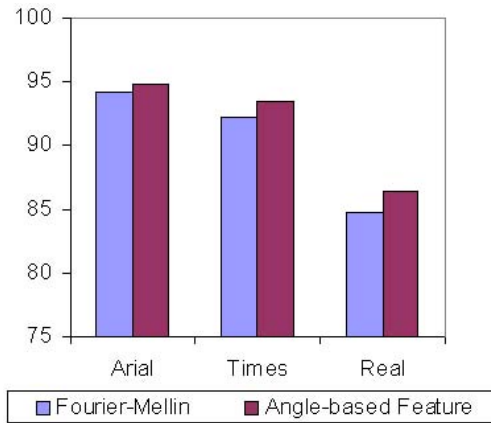


Figure 13: Percentage of touching character segmentation accuracy in datasets of “Arial”, “Times New Roman” fonts and Real dataset.

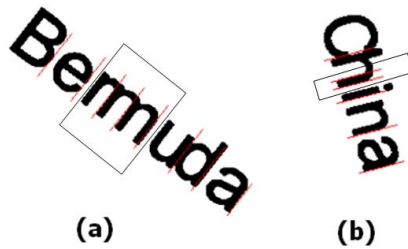


Figure 14: Two examples of wrong segmentation results.

564 *4.4. Experiment on 2-touching Components*

565 Though our objective is to segment n-touching components into their cor-
 566 responding characters, we have performed an experiment with the additional
 567 knowledge of the number of components present in a touching component. This
 568 test is performed to check whether the information of the number of character of
 569 a touching string improves the performance of touching component segmenta-
 570 tion or not. For the experiment, we have created a restricted dataset of touching
 571 components containing 2 characters only. The dataset contains 635 components
 572 (as mentioned in the 2nd row of Table 1) and the characters are in multi-scale
 573 and multi-orientation fashion. The segmentation on this dataset is done based
 574 on the concept discussed in the first paragraph of Section 3. We have obtained
 575 95.74% character segmentation accuracy in this experiment. In Fig.15, we have
 576 shown some touching images with their segmentation results obtained using this
 577 algorithm. From the Table 1, it can be noted that we obtain 92.60% accuracy
 578 on two character touching strings when the number of characters in a touching
 579 string was not known. Thus, it is to be noted that we achieved 3.14% (95.74% -
 580 92.60%) higher accuracy than the dynamic programming based approach when
 581 additional information of the number of characters in a touching component is
 582 used.

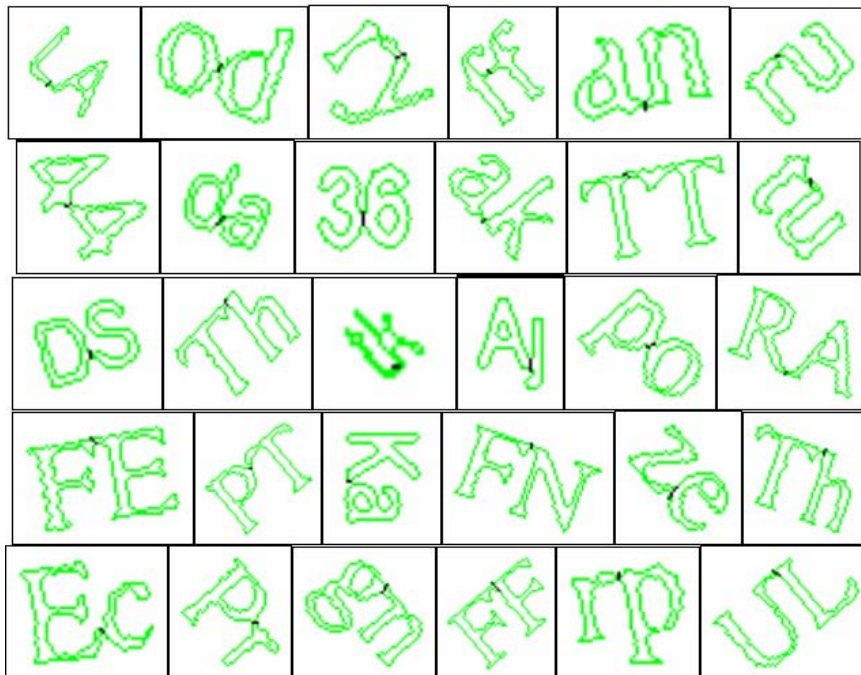


Figure 15: Few images showing segmentation in 2-character touching.

583 *4.5. Experiment on Graphical Documents*

584 We have integrated the touching character segmentation method in OCR of
 585 graphical documents. The details of these graphical documents are mentioned
 586 in Section 4.1. We have performed the character recognition in 10 maps. We

587 show a map in Fig.16. These maps contain text characters at different scale
588 and orientation. There were long graphical lines that touch or overlap with
589 text in these documents. To separate the text components, we remove the long
590 graphical objects that are present in the document using [26]. Also, the text
591 characters in a string sometimes touch together. So, our method of touching
592 character segmentation is applied here for improving character recognition in
593 these documents. The extracted text characters are recognized initially using
594 only isolated character recognition approach. Next, we integrated the touching
595 character segmentation method and compared the recognition accuracy. We
596 show in Table 2 the improvement of OCR in such documents when segmentation
597 based recognition method is used.

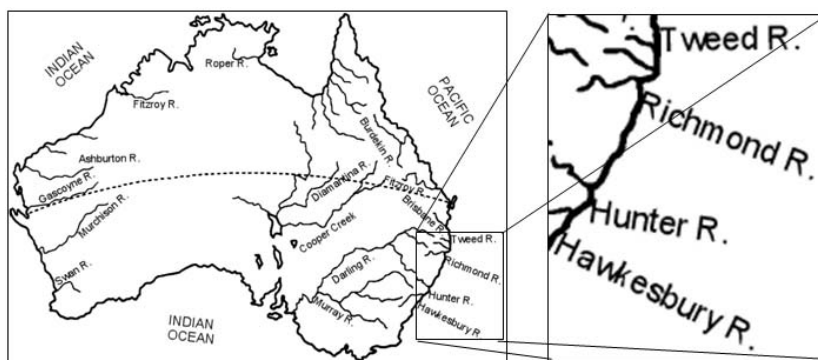


Figure 16: Part of a map showing orientation and touching of characters.

Table 2: Comparison of OCR accuracy by adding touching character segmentation approach

Map Image	Total Number of Characters in the Document	OCR Accuracy without Touching Segmentation	OCR Accuracy with Touching Segmentation
1	251	91.24%	96.81%
2	236	91.95%	95.76%
3	318	92.77%	95.60%
4	458	93.45%	96.07%
5	173	91.33%	96.53%
6	185	87.02%	92.97%
7	201	88.56%	97.01%
8	362	89.50%	95.30%
9	277	97.47%	98.19%
10	180	86.67%	93.89%

598 5. Conclusions

599 In this paper we have proposed a scheme towards segmentation of multi-
600 oriented and multi-sized n-character touching strings. The algorithm, at first,
601 segments the touching characters into primitives and then finds the best se-

602 quence of characters shapes based on a dynamic programming approach using
603 these primitive segments.

604 We also performed an adhoc segmentation approach of touching characters
605 based on the knowledge of number of characters in the touching string. In
606 such a restrictive dataset, we have obtained better performance. But, in a
607 real environment, it is not possible to know a priori the number of characters
608 in the touching component. Hence, the proposed approach based on dynamic
609 programming explores the full idea for such segmentation.

610 To the best of our knowledge, this work is pioneer towards multi-oriented
611 and multi-sized n-character touching string segmentation. We have tested our
612 method on various multi-oriented touching character data with different fonts
613 and scale. As the features of text characters are devised for multi-scale and
614 multi-orientation, some touching characters are not segmented properly due to
615 different possibility of segmentation. Such situation can be taken care of by
616 using a word dictionary in the dynamic programming algorithm and by using
617 contextual information.

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625 Appendix

626 **Douglas-Peucker polyline-approximation algorithm** : The classical
627 Douglas-Peucker [6, 11] polyline-approximation algorithm generates a set of
628 points to represent the original line. It works from top to bottom by starting
629 with a rough initial approximation at a simplified polyline, namely the single
630 edge joining the first and the last vertices of the polyline. Then the remaining
631 vertices are tested for closeness to that edge. If there are vertices further than
632 a specified tolerance, ϵ , away from the edge, then the vertex furthest from it is
633 added to the simplification. This creates a new guess for the simplified polyline.
634 Using recursion, this process continues for each edge of the current guess until
635 all vertices of the original polyline are within the tolerance of the simplification.
636 Fig.17 explains a few steps for obtaining approximated polyline. For a polyline
637 shown in Fig.17(a), the contour pixel (V_t) has the maximum distance from the
638 line joining the farthest points (V_1 and V_n) of the polyline. Next, the polyline
639 is simplified with lines V_1V_t and V_tV_n as shown in Fig.17(b). In Fig.17(c),
640 this process is iterated in polyline segment V_tV_n and V_u is selected having the
641 maximum distance between points V_t and V_n .

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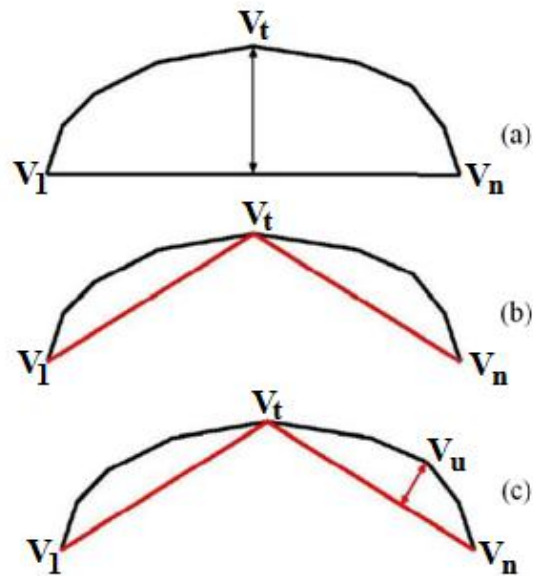


Figure 17: Stages of Douglas-Peucker for Polyline Approximation.

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