



### 3. Methods

The operation of placing each pixel from the ecography to the final world coordinates is described by means of transformation matrices. A pixel with coordinates  $P_{\bar{x}} = (x, y)$  in  $\mathbf{U}$  will be transformed to some other coordinates  $C_{\bar{x}} = (x', y', z')$ :

$$C_{\bar{x}} = P_{\bar{x}} \cdot M_U^R \cdot M_R^T \cdot M_T^C \quad (1)$$

$M_U^R$ , so-called calibration matrix, includes the scaling parameters and the position of the top left corner of the image with regard to the centre of the receiver. Its values are constant provided the receiver's position on the transducer is kept stable and the ecography settings are not changed.

Since the scaling and position parameters are unknown, they must be estimated. Although some papers simply measure the distance between the receiver and the tip of the ecographer, it is much more reliable and precise to compute them statistically by scanning some object with known shape and size. This is known as calibration, and will be described in detail later in this section.

$M_R^T$  contains the position and orientation of the receiver with respect to the transmitter. Therefore, the values will change as the clinician moves the transducer where the receiver is attached.  $M_R^T$  inevitably contains positioning errors, caused by interferences and the limited accuracy of the tracking device.

$M_T^C$  is used for the sake of a proper location, orientation and scaling of the array of voxel system coordinates. After applying  $M_U^R \cdot M_R^T$  to  $P_{\bar{x}}$  in the equation above, the resulting coordinates will likely be some distance away from the coordinate origin, and also the distance between pixels will be set by the tracker specifications.

But in general this will not be adequate; probably, the area to be scanned is rather small compared to the whole volume needed, so we would like to take into account only those coordinates near the scanning. Therefore,  $M_T^C$  will be chosen at user's will, in order to contain the area scanned and with a given scaling and orientation.

In order to calibrate the system, We decided to employ the well known crossing wires method, and to hold the transducer each time a frame had to be captured instead of live video framing. This approach permits to focus properly the field of view to include the point to be imaged, and presumably would reduce the error in positioning the tracker produced by the movement in the previous experiments. Numerical values of the registrations were consistent and reproducible.

Once the system has been calibrated, i.e.,  $M_U^R$  is known, the information (image, position) can be used in many ways. Perhaps the most obvious is to compound a volume image, but others exist. Gee, for instance, in [1] describes a method to resample the data on a curved, not flat, surface, without

actually producing the intermediate image. In the next section we review the process to compound the video sequence into the volume image.

### 4. Compounding the volumes

After the transducer has been calibrated, the spatial information accompanying each image can be employed in many different ways. One way is to combine each video frame with existing images of the same patient, thus providing the surgeon with the ability to complement the information displayed. This idea was explored in another paper [2].

Other possible applications demand the composition of the set of video images into a 3-D image of the scanned volume. The volume image was not compounded while acquiring the data, but the frames and the position were stored in disk. This procedure is very convenient because it permits further experimentation with the data.

We acquired three sequences of data, one for each transducer available. We preferred not to restrict the experiment to a single transducer, in order to obtain more general results.

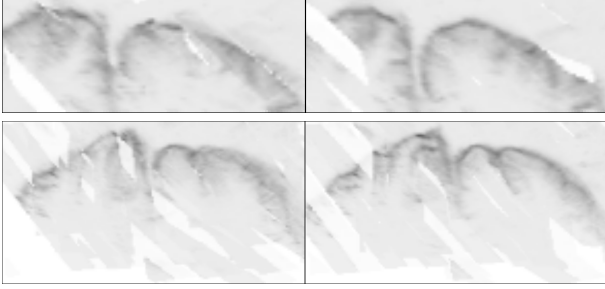
In figure 2 (left column) we depict the compounded volumes for the three probes. Of course, the quality of the images is far from resembling other, more accurate modalities such as MR. However, the contours of the brain and also the sulci are clearly distinguishable, specially for distal slices. Proximal slices show features only at the external borders and around the longitudinal fissure, which are the zones the ultrasound signal could penetrate. No other anatomical issues are exposed, because the shape of the container did not permit any scanning of more proximal areas. Images on right column will be explained in next section.

Note the gaps in the images, in white, which are areas left non scanned. Also note that some areas are clearer than others. The reason is that, despite the correcting effects of taking the mean value, the image contents degrade as more slices are compounded in, and also with stronger positioning error. These areas appear blurred in the final image. In the next section, we will see more closely this effect and one possible way to suppress it.

### 5. Improving accuracy by means of 2-D to 3-D self-registration

The RMS error of the calibration was roughly 3 mm, about 30 pixels. With this numbers, we expected that little could be seen in the composed image. In reality, the positioning error had been overestimated because the composed image was fairly regular and coherent.

Still there was a chance to improve the results: to register each video 2-D image to the compounded 3-D volume.



**Figure 2. Rois of the compounded volume with corrected position (right) compared to the original (left).**

This should be possible also because the Minibird already provides us with an initial estimation of the position of the image in the cuberille. Otherwise, the field of view would probably be too small compared to the size of the volume image to permit any registration. Now, given the initial position, only a small transformation, correcting the positioning errors of tracker, should be expected.

This process is depicted in figure 3: the B-scan during an examination (left) must adjusted to the features already existing in the compounded volume image (right). This adjustment process is called registration: the algorithm will try a explore neighbourhood areas and will choose that with best correspondence.

Following we give the details of the registration algorithm. We have already employed a similar method to other medical image registration, CT to MR volumes [6, 3], and 2D retinographies [4], but the application to 2D–3D registration is a novelty in the subject.

Similarly to any registration algorithm, there were several issues to decide:

- **the model of the transformation to optimise**

We modelled the position error as a rigid transformation given the matrix:

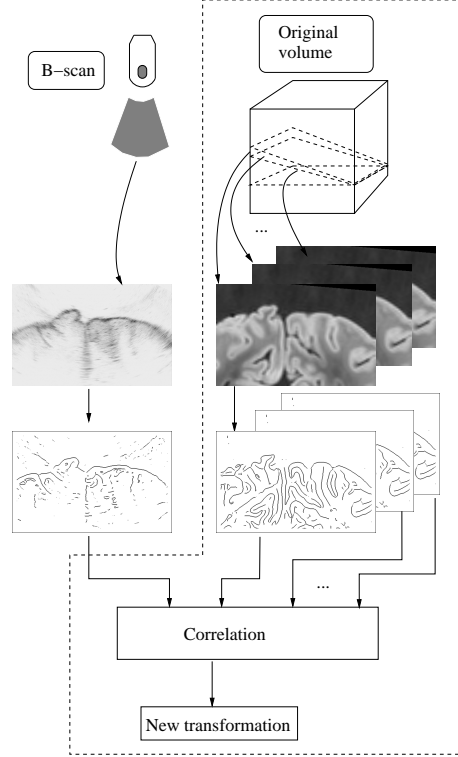
$$M^{ERR} = Tras(T_x, T_y, T_z) * Rot(\phi_x, \phi_y, \phi_z) \quad (2)$$

And we modified equation (1) to include this adjustment:

$$C_{\bar{x}} = P_{\bar{x}} \cdot M^{ERR} \cdot M_U^R \cdot M_R^T \cdot M_T^C \quad (3)$$

The new matrix  $M^{ERR}$  measures the error in the position of the slice.

- **the features to be compared.**



**Figure 3. The iterative registration algorithm.**

The experience of our group was very valuable in this matter; similarly to our previous research, we employed a creaseness operator to extract relevant landmarks. The natural choice was to adapt the already tested algorithms, which worked for 3D–3D and 2D–2D, to work also with 2D–3D. This is, nevertheless, a very suitable choice because again the images to be compared may be very different. The creaseness image suppresses the effect of the gaps and makes them comparable.

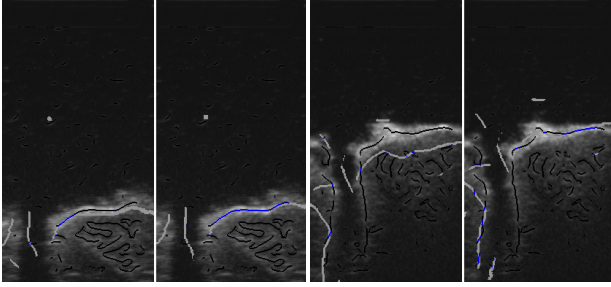
- **the alignment estimation.**

The correlation is suitable function, because it is fast to compute and robust to false and missing features.

- **the scheme of iterative process.**

The iterative step would be the computation of  $\mathcal{C}$ , i.e. the slice to be compared in the cubic image. The iteration would modify the values of  $M^{ERR}$ , which in turn would change the contents of  $\mathcal{C}$ , until the desired convergence has been achieved.

The iterative scheme explained above is too simple to work for real data. In effect, false maxima occur due to artifacts, and the search is bound to get trapped. This problem



**Figure 4. B-scans showing alignment before (left) and after (right) the registration for 10 MHz transducer. Creases are overdrawn in white and black.**

was solved in other papers by means of an exhaustive search in the Fourier domain, which was run on the top level of a hierarchical structure. But this initial step was not suitable now, as the dimensionality of the images was different. Instead, we performed an initial 2d-2d matching.

We run successfully this algorithm for all the series we acquired. An improvement was to compute the target coordinates  $C_{\bar{x}}$  only for non-void pixels  $P_{\bar{x}}$  in the video image, which were usually only 5% of the total. The result was rewarding: the new algorithm ran within 10 seconds per frame.

## 6. Results

Figures 4 show the successful convergence for a few frames. In all figures, the creaseness of  $B$  is depicted over  $B$  in black, and that of the  $C$  in white. Left image corresponds to alignment before registration, right image after registration.

Sometimes, the algorithm fails because the compared creases are too dissimilar. Other times, as seen in last row of the previous figures, large artifacts appearing in  $C$  mislead the search.

We have manually classified each individual registration as valid or non valid, in order to measure the influence of the error described in the last paragraph. We have visually compared the compounded image without and with position correction. To compound the cuberille with the registered values, we have taken the choice to use the original, unregistered transformation, for those frames labelled as not properly registered. This approach permits an easier visualisation of the effects of the registration.

Figure 2 shows a selection of relevant regions of interest for experiment C. Regions shown compare favourably for the self-registered version: the contrast is clearer, there are less artifacts and contours are more continuous. This is

the case for most cases, but occasionally the contrary also happens when the field of view is smaller.

## 7. Conclusions and future work

Our contribution in this paper has consisted on a new method to correct motion errors when compound 3D ultrasound images. The method is fast and fully automatic, and has proved acceptable accuracy. Also, we have specified the steps necessary to achieve a proper calibration of the transducer. As a future work, we plan design a filter to automatically discard wrong registration: the set of transformations obtained follows a regular fashion, thus those too large or with non-coherent directions will be safely discarded.

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